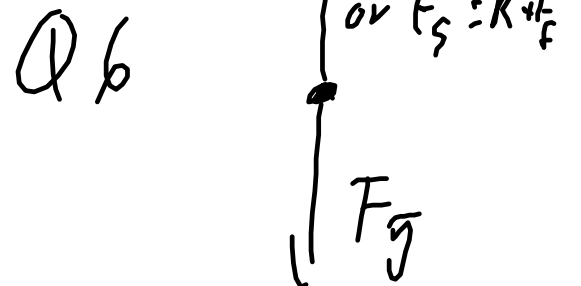
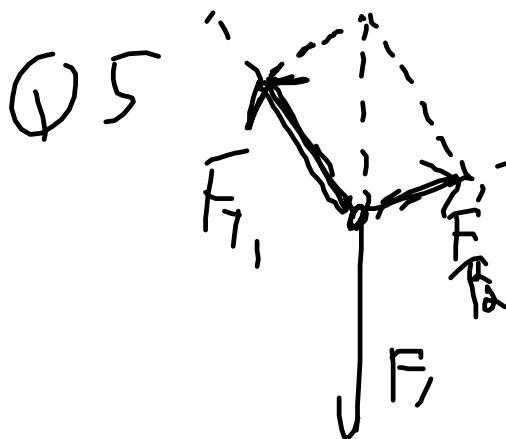
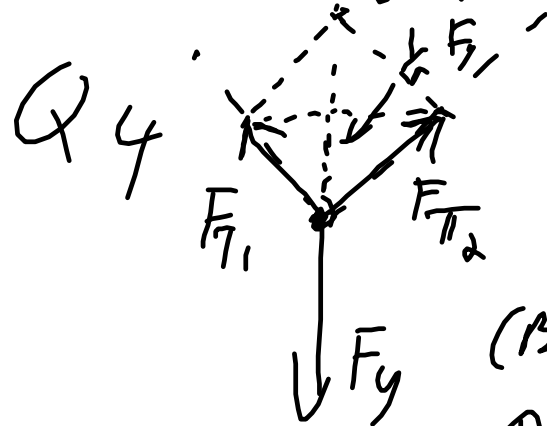
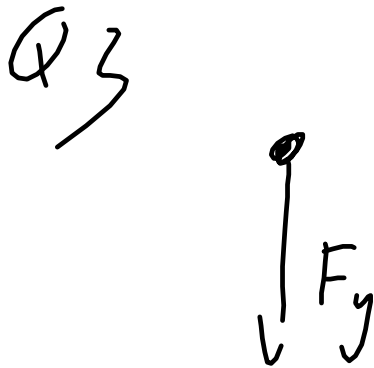
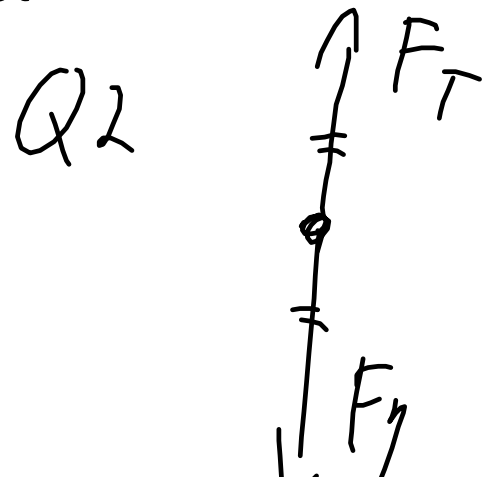
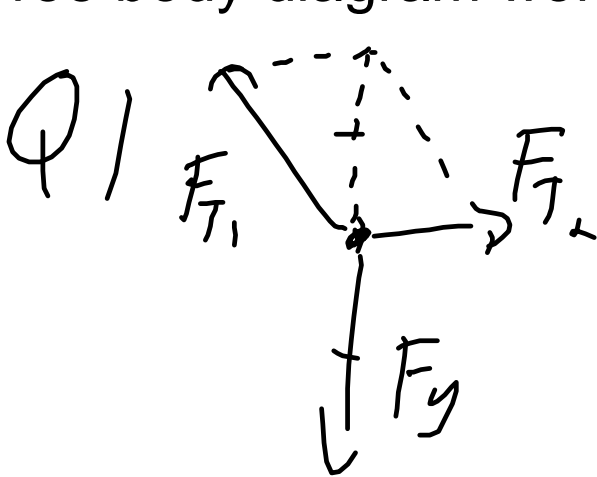


# Free body diagram worksheet



$F_s = \text{Surface Force} = F_f + R$





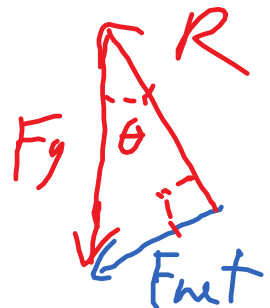
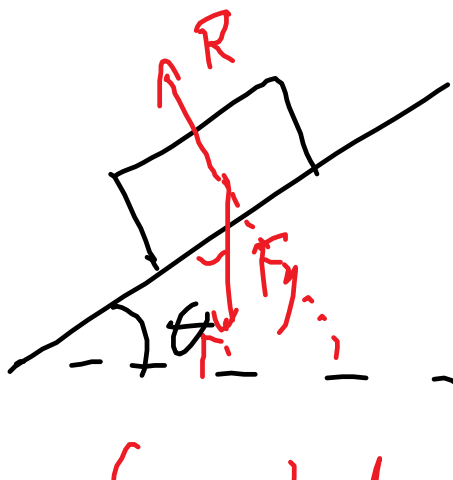
## Slopes and Pulleys

Determine the net force and acceleration of blocks on slopes and masses connected by pulleys.

Start with Free body diagram of forces, convert to a vector addition diagram (head to tail) and calculate resultant using trig - cosine law or components.

Look at a block on a slope. What is the acceleration of the block if the slope is

- a) frictionless
- b) coefficient of static friction  $\mu_s$  and kinetic friction,  $\mu_k$ .
- c) the block is connected over a pulley to another block



Vector Addition

free body

Vector Addition

$$F_{\text{net}} = F_g \sin \theta$$

Component of  $F_g$  parallel to the slope

$$F_{g\parallel} = F_g \sin \theta$$

$$R = F_g \cos \theta$$

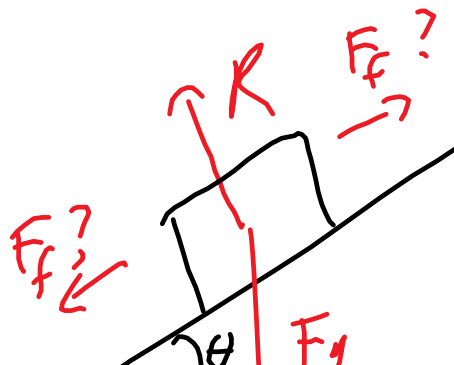
Perpendicular component of  $F_g$

$$F_{g\perp} = F_g \cos \theta$$

$$a = \frac{F_{\text{net}}}{m} = \frac{mg \sin \theta}{m}$$

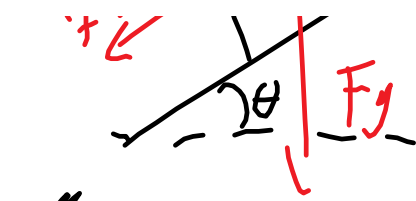
$$a = g \sin \theta$$

b)



$F_{fk}$  is opposite velocity

$F_r$  is opposite



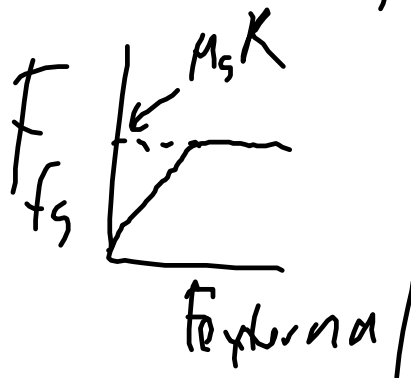
$F_{fs}$  is opposite external forces



$$F_{fk} = \mu_k R$$

$$F_{fs} \leq \mu_s R$$

depends on external forces



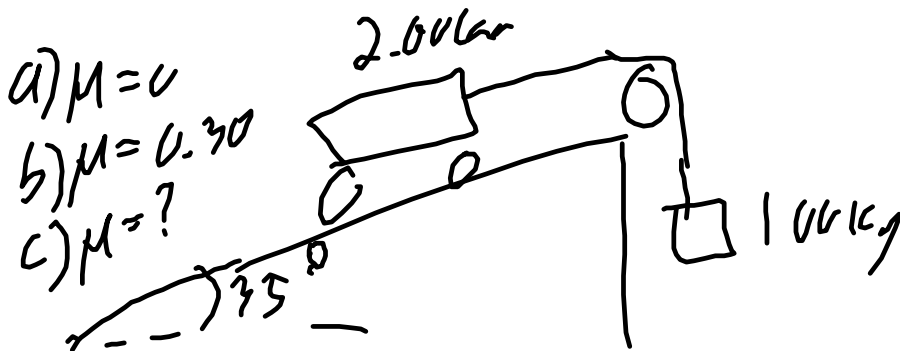
$$F_{net} = \sum F_{||} = F_{g||} (\pm) F_f$$

$$ma = mg \sin \theta \pm \mu mg \cos \theta$$

$$a = g \sin \theta \pm \mu g \cos \theta$$

A 2.00 kg cart is on a 35.0° slope.  
Determine the acceleration of the cart if  
a) it is frictionless

- b) the friction in the wheels corresponds to a coefficient of 0.30.
- c) what coefficient of static friction would prevent rolling?
- d) the 2.00kg cart is connected by a string up the slope over a pulley to a 1.00 kg mass hanging off the table. Answer a,b,and c again.



$$T = 2\pi \sqrt{\frac{l}{g}} = 2\pi \sqrt{\frac{0.481\text{m}}{9.81\frac{\text{m}}{\text{s}^2}}}$$

$$= \frac{\text{m} \div \text{m}}{\text{s}^2}$$

$$\cancel{\text{m}} \times \frac{\text{s}^2}{\cancel{\text{m}}}$$

$$b) \chi = 0.30\text{m} \cos(3.14 +)$$

$$\omega = \frac{2\pi}{T}$$

Radians

$$c) V_{\max} = \omega x_0 = 3.14 \times 0.3 = 0.94 \text{ m/s}$$

$$d) V = V_{\max} \sin \omega t$$

$$V = 0.94 \sin \{3.14(0.25)\}$$

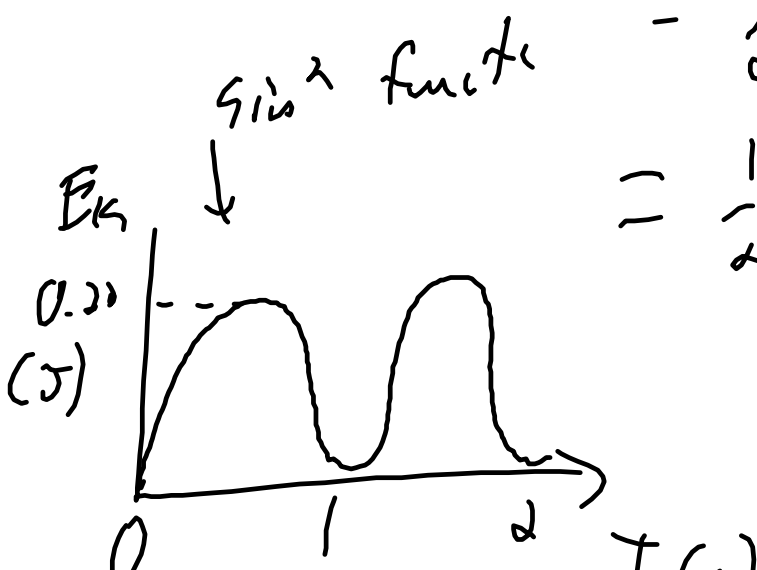
$$= 0.67 \text{ m/s}$$

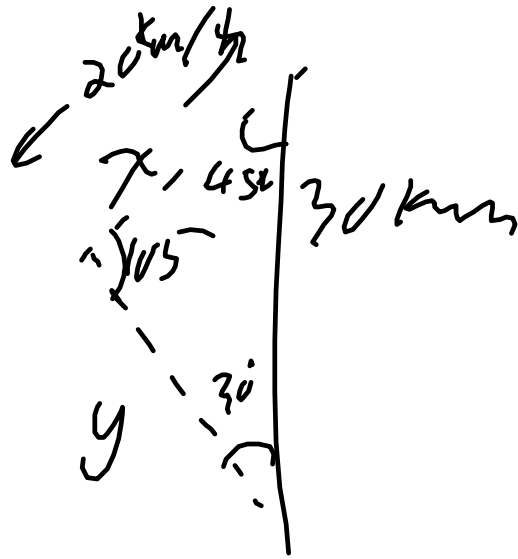
$$E_k = \frac{1}{2} m v^2 = \frac{1}{2} m (\omega \sqrt{x_0^2})^2$$

$$= \frac{1}{2} m \omega^2 x_0^2$$

$$= \frac{1}{2} (0.5) (3.14)^2 (0.3)^2$$

$$= \boxed{0.22 \text{ J}}$$





$$\frac{\sin 30}{x} = \frac{\sin 105}{30}$$

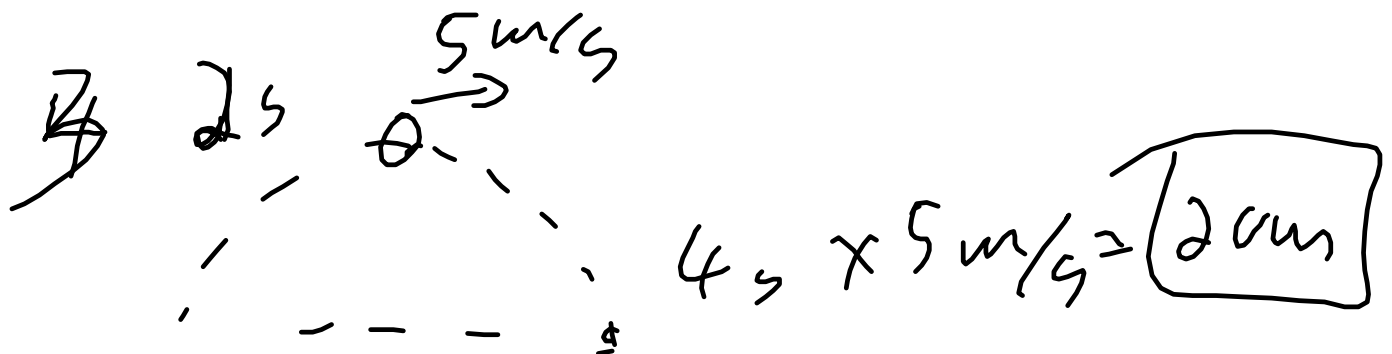
$$x = d$$

$$t = \frac{d}{20 \text{ km/h}}$$

$$\frac{\sin 45}{y} = \frac{\sin 105}{30}$$

$$V = \frac{d}{t} = 20 \text{ km/h}$$

$$20 \sin 45 = V \sin 30$$



4)

$$V \sin \theta = v_y$$

$$s = \frac{1}{1 - 120} \quad \frac{1}{1}$$

$$s_x = 760 \text{ m}$$